

7.1 Rational Exponents

ALGEBRA 2

Write your
questions here!



Review of Exponents:

$8^3 =$

$8^{-3} =$

$8^{\frac{1}{3}} =$

Rewrite each in radical form:

Ex 1)

Ex 2)

Ex 3)

Rewrite each using a base that is an integer.

Ex 4)

Ex 5)

Ex 6)

Simplify:

Ex 7)

Ex 8)

Ex 9)

Ex 10)

Ex 11)

Ex 12)

Solve for x:

Ex 13)

Ex 14)

Ex 15)

Ex 16) $\sqrt{\sqrt[3]{(a+1)^5}} = (a+1)^x$

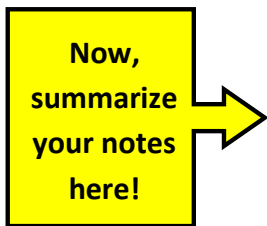
Can you solve these?:

The expression $\sqrt{a^2 b^3}$ is equivalent to $a^x b^y$ where a and b are both positive. Find the value of x ?

Which function is equivalent to $F(x) = \frac{\sqrt{(x-2)}}{\left(x^{\frac{1}{4}}\right)^2}$ for all positive values of x?

- a. $G(x) = \sqrt[3]{x^2}$ b. $H(x) = \sqrt[2]{x^3}$ c. $K(x) = -\sqrt[3]{x^2}$ d. $J(x) = \frac{1}{\sqrt[2]{x^3}}$

SUMMARY:



7.1 Rational Exponents

7.1 PRACTICE

Directions: Write each expression in exponential form.			
1) $\sqrt{6x}$	2) $\frac{1}{\sqrt{m}}$	3) $(\sqrt[4]{5n})^5$	4) $(\sqrt[3]{-27g})^2$
Directions: Write each expression in radical form.			
5) $(4m)^{5/3}$	6) $(-5x)^{7/4}$	7) $n^{1/3}$	8) $(8y)^{-3/4}$

Simplify.			
9) $\sqrt[3]{-64}$	10) $(\sqrt[3]{-27})^{-4}$	11) $81^{3/2}$	12) $36^{3/2}$
13) $(-125)^{-2/3}$	14) $81^{-3/2}$	15) $125^{1/3}$	16) $343^{4/3}$

17. Which expression is equivalent to $\sqrt{5^8}$? a. $5^{\frac{1}{3}}$ b. 5^3 c. 5^4 d. 5^6

A	B	C	D
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

18. Which expression is equivalent to $\frac{\sqrt[3]{5^2}}{\left(\frac{1}{5^3}\right)^2}$? a. $5^{\frac{2}{3}}$ b. 1 c. 0 d. 5

A	B	C	D
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Multiple Choice!
Choose the BEST
answer!

19. The expression 27^x is equivalent to 9^y where x and y are both positive. Find the value of $\frac{x}{y}$?

20. If $2^x \cdot 2^y = \sqrt[3]{2}$ and $x = \frac{1}{2}$, what is the value of y ?

21. If $3x^3 = y^{12}$, solve for x in terms of y , in radical form.

22. If k, n, x and y are positive values satisfying $x^{\frac{-4}{3}} = k^{-2}$ and $y^{\frac{4}{3}} = n^2$, what is $(xy)^{\frac{2}{3}}$ in terms of n and k ?

Solve the following equations:

23. $2x^{\frac{2}{3}} - 7 = 11$

24. $9^{2x-5} = 27$

25. $25^{2x-1} = 125^{3x+4}$

26. $(\sqrt{x})^4 = 25$

27. $64^{2x} = 16$

28. $\sqrt{\sqrt[4]{(k-21)^5}} = (k-21)^x$

29. $\sqrt[3]{x+4} = 2$

30. $5 = 3 + \sqrt[4]{2x+1}$

7.1 Rational Exponents

WRAP UP

1. $5x^{\frac{2}{3}} + 4 = 24$

2. $(\sqrt[3]{2})^9 = 16^x$

3. Simplify: $(-125)^{-1/3}$

Extension: Simplify:

4. $(2^{\sqrt{3}})^{\sqrt{3}}$

5. $(2^{\sqrt{2}})^{\sqrt{2}} (3^{\sqrt{3}})^{\sqrt{3}}$

6. $(3^{1+\sqrt{2}})^{1-\sqrt{2}}$

7. **Test PREP!** One is multiple choice; the other is free response where you must grid in your answer. Blow it up.

MULITPLE CHOICE	GRID IN																																																								
<p>a. If n and p are positive integers and $2^{n/p} = \sqrt[3]{32}$, then the product of n and p is:</p> <p>(A) -16 (B) 15 (C) 14 (D) 18</p> <p style="text-align: center;"><i>Grid your answer here ↓</i></p> <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td style="padding: 2px 5px;">A</td> <td style="padding: 2px 5px;">B</td> <td style="padding: 2px 5px;">C</td> <td style="padding: 2px 5px;">D</td> </tr> <tr> <td style="text-align: center;"><input type="radio"/></td> <td style="text-align: center;"><input type="radio"/></td> <td style="text-align: center;"><input type="radio"/></td> <td style="text-align: center;"><input type="radio"/></td> </tr> </table>	A	B	C	D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<p>b. If $p^m \cdot p^{-5} = p^{10}$, and $(p^{-3})^n = p^{-21}$, what is the value of $m - n$?</p> <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse; text-align: center;"> <tr> <td style="width: 20px; height: 20px;"></td> <td style="width: 20px; height: 20px;">/</td> <td style="width: 20px; height: 20px;">/</td> <td style="width: 20px; height: 20px;"></td> </tr> <tr> <td style="width: 20px; height: 20px;">•</td> <td style="width: 20px; height: 20px;">•</td> <td style="width: 20px; height: 20px;">•</td> <td style="width: 20px; height: 20px;">•</td> </tr> <tr> <td style="width: 20px; height: 20px;">0</td> <td style="width: 20px; height: 20px;">0</td> <td style="width: 20px; height: 20px;">0</td> <td style="width: 20px; height: 20px;">0</td> </tr> <tr> <td style="width: 20px; height: 20px;">1</td> <td style="width: 20px; height: 20px;">1</td> <td style="width: 20px; height: 20px;">1</td> <td style="width: 20px; height: 20px;">1</td> </tr> <tr> <td style="width: 20px; height: 20px;">2</td> <td style="width: 20px; height: 20px;">2</td> <td style="width: 20px; height: 20px;">2</td> <td style="width: 20px; height: 20px;">2</td> </tr> <tr> <td style="width: 20px; height: 20px;">3</td> <td style="width: 20px; height: 20px;">3</td> <td style="width: 20px; height: 20px;">3</td> <td style="width: 20px; height: 20px;">3</td> </tr> <tr> <td style="width: 20px; height: 20px;">4</td> <td style="width: 20px; height: 20px;">4</td> <td style="width: 20px; height: 20px;">4</td> <td style="width: 20px; height: 20px;">4</td> </tr> <tr> <td style="width: 20px; height: 20px;">5</td> <td style="width: 20px; height: 20px;">5</td> <td style="width: 20px; height: 20px;">5</td> <td style="width: 20px; height: 20px;">5</td> </tr> <tr> <td style="width: 20px; height: 20px;">6</td> <td style="width: 20px; height: 20px;">6</td> <td style="width: 20px; height: 20px;">6</td> <td style="width: 20px; height: 20px;">6</td> </tr> <tr> <td style="width: 20px; height: 20px;">7</td> <td style="width: 20px; height: 20px;">7</td> <td style="width: 20px; height: 20px;">7</td> <td style="width: 20px; height: 20px;">7</td> </tr> <tr> <td style="width: 20px; height: 20px;">8</td> <td style="width: 20px; height: 20px;">8</td> <td style="width: 20px; height: 20px;">8</td> <td style="width: 20px; height: 20px;">8</td> </tr> <tr> <td style="width: 20px; height: 20px;">9</td> <td style="width: 20px; height: 20px;">9</td> <td style="width: 20px; height: 20px;">9</td> <td style="width: 20px; height: 20px;">9</td> </tr> </table>		/	/		•	•	•	•	0	0	0	0	1	1	1	1	2	2	2	2	3	3	3	3	4	4	4	4	5	5	5	5	6	6	6	6	7	7	7	7	8	8	8	8	9	9	9	9
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8. Show that $(\sqrt{x} + \sqrt{y})^2$ is not equal to $(x^1 + y^1)$ when $x = 9$ and $y = 16$.

(Out of this world) EXIT TICKET!

Kepler's third law of planetary motion relates the average distance of a planet from the sun to the time it takes the planet to complete one full orbit around the sun. The equation $t^2 = a^3$ describes the law where a is the distance the planet is from the sun and t is the time measured in (Earth) years. The distance a is measured in AUs, which is the average distance from the sun to the Earth.

a) Solve the equation for a .



Answer: $a =$

b) Venus takes about 0.62 Earth years to orbit the sun. Use your answer to a) to find the average distance from the sun to Venus.

Answer: _____ AUs

c) Mercury is about .39AUs from the sun. About how many days does it take for Mercury to orbit the sun?

Answer: _____ days