

4.2 Multiply and Divide Radicals

PRACTICE

Directions: Multiply.

1) $\sqrt{2}(3 - 2\sqrt{10})$

$$\begin{aligned} & 3\sqrt{2} - 2\sqrt{20} \\ & 3\sqrt{2} - 2\sqrt{4\sqrt{5}} \\ & 3\sqrt{2} - 2 \cdot 2\sqrt{5} \\ & \boxed{3\sqrt{2} - 4\sqrt{5}} \end{aligned}$$

2) $-4\sqrt{7}(4\sqrt{14} + 3\sqrt{7})$

$$\begin{aligned} & -16\sqrt{98} - 12\sqrt{49} \\ & -16\sqrt{49\sqrt{2}} - 12 \cdot 7 \\ & -16 \cdot 7\sqrt{2} - 84 \\ & \boxed{-112\sqrt{2} - 84} \end{aligned}$$

3) $(2\sqrt{10} - 3\sqrt{2})(\sqrt{10} + 4\sqrt{2})$

$$\begin{aligned} & 2\sqrt{100} + 8\sqrt{20} - 3\sqrt{20} - 12\sqrt{4} \\ & = 2 \cdot 10 + 8\sqrt{4\sqrt{5}} - 3\sqrt{4\sqrt{5}} - 12 \cdot 2 \\ & = 20 + 8 \cdot 2\sqrt{5} - 3 \cdot 2\sqrt{5} - 24 \\ & = -4 + 16\sqrt{5} - 6\sqrt{5} \\ & = \boxed{-4 + 10\sqrt{5}} \end{aligned}$$

4) $(5\sqrt{6} - 8\sqrt{12})(2\sqrt{15} - \sqrt{2})$

$$\begin{aligned} & 10\sqrt{90} - 5\sqrt{12} - 16\sqrt{180} + 8\sqrt{24} \\ & 10\sqrt{9\sqrt{10}} - 5\sqrt{4\sqrt{3}} - 16\sqrt{36\sqrt{5}} + 8\sqrt{4\sqrt{6}} \\ & 10 \cdot 3\sqrt{10} - 5 \cdot 2\sqrt{3} - 16 \cdot 6\sqrt{5} + 8 \cdot 2\sqrt{6} \\ & \boxed{30\sqrt{10} - 10\sqrt{3} - 96\sqrt{5} + 16\sqrt{6}} \end{aligned}$$

Directions: Choose the best answer. SHOW WORK.

5) Multiply: $\sqrt[3]{4}(2\sqrt[3]{6} + 5\sqrt[3]{32})$

$$\begin{aligned} & \text{a. } \sqrt[3]{3} + 20\sqrt[3]{2} \\ & \text{b. } 2\sqrt[3]{24} + 5\sqrt[3]{128} \\ & \text{c. } 4\sqrt[3]{3} + 20\sqrt[3]{2} \\ & \text{d. } \boxed{4\sqrt[3]{3} + 20\sqrt[3]{2}} \end{aligned}$$

$$\begin{aligned} & 2^3\sqrt[3]{24} + 5^3\sqrt[3]{128} \\ & 2^3\sqrt[3]{8\sqrt[3]{3}} + 5^3\sqrt[3]{64\sqrt[3]{2}} \\ & 2 \cdot 2^3\sqrt[3]{3} + 5 \cdot 4^3\sqrt[3]{2} \\ & 4\sqrt[3]{3} + 20\sqrt[3]{2} \end{aligned}$$

6) Divide: $\frac{(\sqrt{21}-\sqrt{3})\sqrt{3}}{\sqrt{3}\sqrt{3}} = \frac{\sqrt{63} - \sqrt{9}}{\sqrt{9}}$

$$\begin{aligned} & \text{a. } \sqrt{21} \\ & \text{b. } \boxed{\sqrt{7} - 1} \\ & \text{c. } \frac{\sqrt{63}-3}{3} \\ & \text{d. } \frac{3\sqrt{7}-3}{3} \end{aligned}$$

$$\begin{aligned} & = \frac{\sqrt{9\sqrt{7}} - 3}{\sqrt{9}} \\ & = \frac{3\sqrt{7} - 3}{3} = \frac{3(\sqrt{7}-1)}{3} \end{aligned}$$

Directions: Divide

7) $\frac{5\sqrt{10}}{\sqrt{10}\sqrt{10}}$

$$= \frac{5\sqrt{10}}{10} = \boxed{\frac{\sqrt{10}}{2}}$$

8) $\frac{\sqrt{6}\sqrt{8}}{2\sqrt{8}\sqrt{8}} = \frac{\sqrt{48}}{2 \cdot 8} = \frac{\sqrt{16\sqrt{3}}}{16}$

$$\begin{aligned} & = \frac{4\sqrt{3}}{16} \\ & = \boxed{\frac{\sqrt{3}}{4}} \end{aligned}$$

9) $\frac{(6+\sqrt{35})\sqrt{5}}{\sqrt{5}\sqrt{5}}$

$$\begin{aligned} & = \frac{6\sqrt{5} + \sqrt{175}}{5} \\ & = \frac{6\sqrt{5} + \sqrt{25\sqrt{7}}}{5} \\ & = \boxed{\frac{6\sqrt{5} + 5\sqrt{7}}{5}} \end{aligned}$$

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<p>10) $\frac{10}{2-\sqrt{7}} \cdot \frac{(2+\sqrt{7})}{(2+\sqrt{7})}$</p> <p>$= \frac{20 + 10\sqrt{7}}{4 - 7}$</p> <p>$= \frac{20 + 10\sqrt{7}}{-3}$</p>	<p>11) $\frac{2-\sqrt{2}}{\sqrt{6}+\sqrt{2}} \cdot \frac{(\sqrt{6}-\sqrt{2})}{(\sqrt{6}-\sqrt{2})}$</p> <p>$= \frac{2\sqrt{6} - 2\sqrt{2} - \sqrt{12} + \sqrt{4}}{6 - 2}$</p> <p>$= \frac{2\sqrt{6} - 2\sqrt{2} - \sqrt{4}\sqrt{3} + 2}{4}$</p> <p>$= \frac{2\sqrt{6} - 2\sqrt{2} - 2\sqrt{3} + 2}{4}$</p> <p>$= \frac{\sqrt{6} - \sqrt{2} - \sqrt{3} + 1}{2}$</p>	<p>12) $\frac{2\sqrt{3}-\sqrt{5}}{\sqrt{5}+\sqrt{6}} \cdot \frac{(\sqrt{5}-\sqrt{6})}{(\sqrt{5}-\sqrt{6})}$</p> <p>$= \frac{2\sqrt{15} - 2\sqrt{18} - \sqrt{15} + \sqrt{30}}{5 - 6}$</p> <p>$= \frac{2\sqrt{15} - 2\sqrt{6}\sqrt{2} - 5 + \sqrt{30}}{-1}$</p> <p>$= -2\sqrt{15} + 2\sqrt{6}\sqrt{2} + 5 - \sqrt{30}$</p> <p>$= -2\sqrt{15} + 6\sqrt{2} + 5 - \sqrt{30}$</p>
<p>Directions: Factor.</p>		
<p>13) $4h^2 - 13h - 12$ $\times -48$</p> <p>$(4h^2 - 16h) + (3h - 12) + 13$</p> <p>$4h(h-4) + 3(h-4)$</p> <p>$(h-4)(4h+3)$</p>	<p>14) $28y^3 + 24y^2(-35y - 30)$</p> <p>$4y^2(7y+6) - 5(7y+6)$</p> <p>$(7y+6)(4y^2-5)$</p>	<p>15) $2x^4 - 19x^2 + 9$ $\times 18$</p> <p>$(2x^4 - 18x^2) - 1(x^2 + 9) - 19$</p> <p>$2x^2(x^2-9) - 1(x^2-9)$</p> <p>$(x^2-9)(2x^2-1)$</p> <p>$(x-3)(x+3)(2x^2-1)$</p>